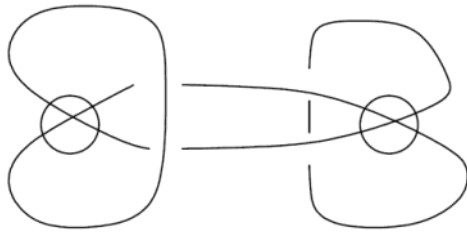


# A Kishino Braid

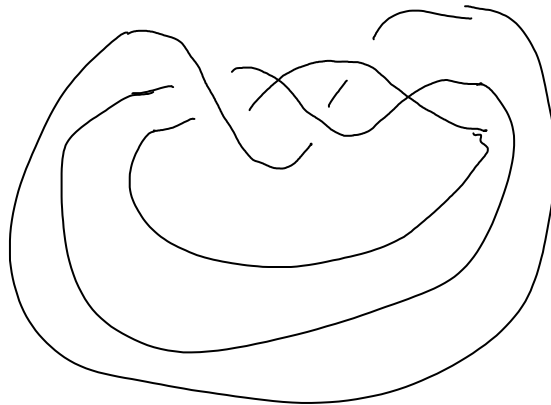
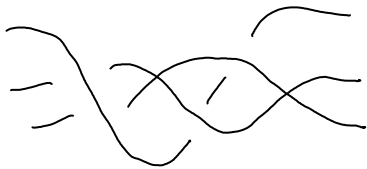
December-05-08  
1:38 PM

Image from  
**Title:** Virtual knots undetected by 1 and 2-strand  
bracket polynomials  
**Authors:** H. A. [Dye](#)

Pasted from <<http://front.math.ucdavis.edu/0402.5308>>



Kishino's Knot



Non trivial

Oops, with  $B = \overbrace{\underbrace{\quad}^x}_{\quad}$  we seem to have

$$B^2 = I, \text{ yet } B \neq I.$$

$$I \ni (B-I)(B-I) = B^2 - 2B + I = 2I - 2B$$

$$\nRightarrow B-I=0 \text{ in } \text{proj } V_B$$

except  $B$  has a non-trivial skeleton.

$$\underbrace{\supset \subset}_{\supset \subset}$$

$$\underbrace{\supset \subset}_{\supset \subset}$$

OK, Questions:

1. Prove that

$$\left[ \overbrace{\underbrace{\quad}^x}_{\quad}, \overbrace{\underbrace{\quad}^x}_{\quad} \right] \text{ is non-trivial in } V_B.$$

will it work using the Jones polynomial?

2, Prove that

$$\left[ \left[ \left| \leftarrow \right|, \leftarrow \right| \right], \left[ \left| \rightarrow \right|, \rightarrow \right| \right] \right]$$

is non-trivial in  $A_3^V$

3. Aside Is the Kauffman bracket of a virtual knot of finite type? What is its weight system?

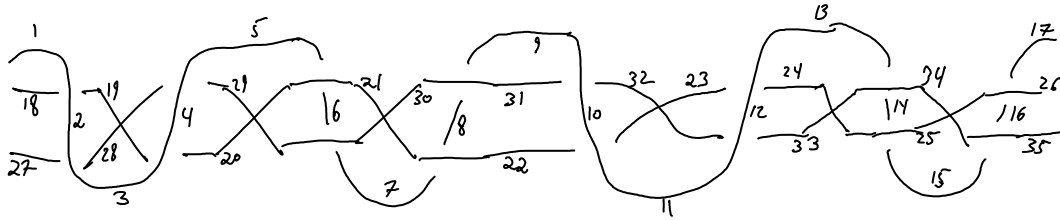
"of" means "dominated by".

— It is not obviously of finite type:

$$\bigcirc \rightarrow \bigvee - \bigwedge \rightarrow \pm q \bigcirc \pm \bigvee \pm \bigwedge$$

and there are no cancellations at  $q=1$ .

Likewise, what's the relationship between the Jones polynomial and the Kauffman bracket for  $v$ -knots?



Just for comparison, a trivial braid:

