

Geodesics in Hyperbolic Geometry

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Snell's law:

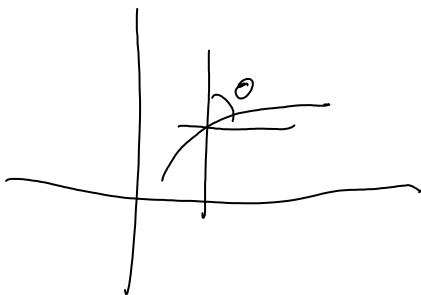
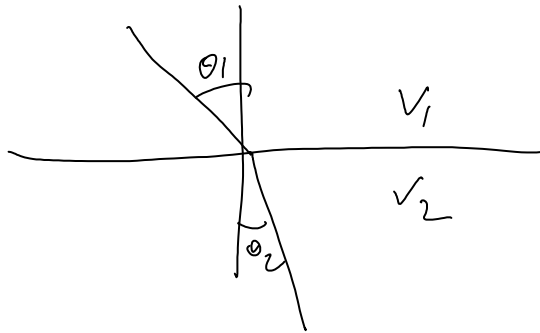
$$\frac{\sinh \theta_1}{\sinh \theta_2} = \frac{v_1}{v_2}$$

or

$$\frac{\sinh \theta_1}{v_1} = \frac{\sinh \theta_2}{v_2}$$

$$\text{or } \frac{\sinh \theta}{v} = C$$

$$\text{or } \frac{v}{\sinh \theta} = C$$



$$V = y$$

$$y' = \frac{\cos \theta}{\sinh \theta} = \frac{\sqrt{1 - \sinh^2 \theta}}{\sinh \theta}$$

$$(\sinh \theta) y' = \sqrt{1 - \sinh^2 \theta}$$

$$\sinh^2 \theta (y')^2 = 1 - \sinh^2 \theta$$

$$\sinh^2 \theta (1 + y'^2) = 1$$

$$\sinh \theta = \sqrt{\frac{1}{1 + (y')^2}}$$

$$\Rightarrow C = \frac{y}{\sqrt{\frac{1}{1 + (y')^2}}} = y \sqrt{1 + (y')^2}$$

$$\frac{v}{\sinh \theta} = C$$

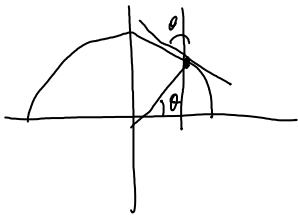
$$v = y$$

$\sinh t, \cosh t$



$$\frac{y}{x} = \frac{\cosh \theta}{\sinh \theta} = \frac{\cosh \theta}{\sinh \theta}$$

$$\frac{\cosh t}{-\sinh t} =$$



$$\frac{\sin \theta}{\sin \theta} = 1 \quad \checkmark$$